Elimination Round 1

1	If $\begin{bmatrix} 2 & 3 & 5 \\ 0 & 6 & 4 \\ 0 & 0 & 1 \end{bmatrix}\begin{bmatrix} 1 & 4 & 2 \\ 0 & 3 & 5 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix}$, what is $d + g + h$?	0
2	What is the smallest positive integer that has a remainder of 2 when divided by 5, a remainder of 4 when divided by 7, and a remainder of 6 when divided 9?	312
3	If $x = \sqrt{-1}$, evaluate the following: $$\frac{x^{17} - 1}{x - 1}$$	1
4	Name one possible positive integer n for which $n^2 - n + 41$ is composite.	$41, 42, 82, 83,$ or any $n = 0$ or $1 \bmod 41$
5	In a triangle of side lengths 5, 12, and 13, what is the product of the radii of the incircle and the circumcircle?	13
6	On a 24-hour analog clock, the hour hand completes one revolution in 24 hours instead of 12, and the minute hand completes one revolution in 60 minutes, as usual. At what time or times where the hour and minutes are both integers do the minute and hour hands perfectly overlap?	0 hours, 12 hours, 24 hours, …
7	Let $f(x) = x^3 - 2x^2 + 3x - 4$ and $g(x) = x - 4$. What is the sum of $f(4)$ and the remainder of $\frac{f(x)}{g(x)}$?	80
8	In $\triangle ABC$, $m\angle CBA = 60°$, $BC = 7$, and $AC = \sqrt{39}$. Find the length of AB.	Either 2 or 5
9	For what positive integer value of x is the inequality $(x + 10)^2 \le (x - 12)^2$ satisfied?	1
10	What is the lateral surface area of the cone formed from a 252-degree sector of a 10-inch radius circle by aligning the two straight sides?	70π

EX	**Extra Question (only if needed):** The parabola $y = ax^2 + bx + c$ has vertex $(1, 1)$ and y-intercept $(0, -1)$. What is the value of b?	4