

1. (Without using calculus) Determine the slope (m) of the tangent line " $y = mx + 2$ " to the parabola " $y = x^2 + 5x + 6$ ".
2. Let f be a real-valued function such that

$$f(x) + 2f\left(\frac{2002}{x}\right) = 3x$$

for all $x > 0$. Find $f(2)$.

Problem Solving Method 3:

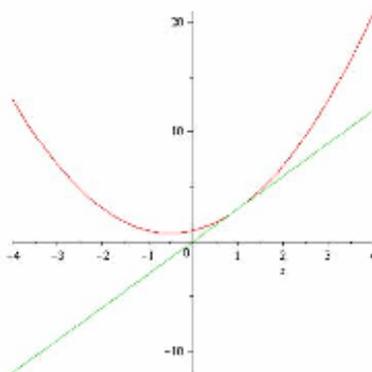
Change the problem to one you know how to deal with

Example: Determine the slope (m) of the tangent line " $y = mx + 2$ " to the parabola " $y = x^2 + 5x + 6$ ".

- What you might not know: Calculus
- What you do know: Algebra and Geometry

Normally, the *derivative* is used in this situation to find tangent slopes to a function, which is in this case a parabola. However, we can change the problem to one that is easier to deal with by simply observing the definition of a tangent line:

A tangent line intersects a function in only one spot



Thus, we can solve for the slope m by setting the equations $y = mx + 2$ and $y = x^2 + 5x + 6$ equal to each other and giving m a value that makes the solution a complete square.